Separate measurement of the $5f_{5/2}$ and $5f_{7/2}$ unoccupied density of states of UO$_2$

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ABSTRACT

Coupling High Energy Resolution Fluorescence Detection (HERFD) with electric dipole selection rules, the uranium $5f_{5/2}$ and $5f_{7/2}$ Unoccupied Densities of States (UDOS) have been determined in UF$_4$, UO$_2$ and UCd$_{11}$. Striking changes were observed between UF$_4$ ($5f^2$) to UCd$_{11}$ ($5f^3$), consistent with the Intermediate Coupling Model. Results for UO$_2$ were confirmed by Bremstrahlung Isochromat Spectroscopy (BIS). This new approach can be a powerful tool for shedding light on the hidden mysteries of Actinides 5f-electrons properties.

1. Introduction

The 5f series of elements known as the actinides have vast technological and scientific importance in today’s world, notably in energy technologies [1], weapons production and associated environmental remediation [2], and medicine [3]. In particular, understanding the environmental impacts of certain actinides has become a major concern due to the buildup of nuclear waste [4]. Despite their technological importance, the chemistry and physics of the actinides remain the least understood of the long-lived elements in the periodic table. Some of the lack of understanding of the bonding properties of the actinides is due to their relative unavailability, but the primary issue is actually the complexity of the bonding properties of the 5f orbital [5]. At the heart of this complexity is the importance of spin-orbit coupling and relativity in determining electron distributions [6]. From a practical standpoint, unlike 4f orbitals, the 5f orbital can be delocalized, especially for the actinides lighter than Am [7]. On the other hand, the 5f’s can also be localized, but even in these cases, covalent bonds can still exist [8]. Moreover, most of the actinides can exist in multiple oxidation states (5f occupancies), with Pu known to exist in many states from, at least, Pu (III) to Pu (VII) [9]. This interplay between orbital occupancy and delocalization affects not only the chemical structures of the actinides and their compounds, but also all their electronic and magnetic properties [10]. Despite the importance of determining the 5f orbital density of states, occupancy and degree of delocalization, such measurements of these properties have proved elusive. Photoemission spectroscopies are sometimes successful, but suffer from experimental difficulties and surface sensitivity [11]. Conventional X-Ray Absorption Spectroscopy and a related technique, Electron Energy Loss Spectroscopy (EELS), especially when coupled to branching ratio analysis [12], are likewise useful but suffer from the limitations imposed by the lifetime broadenings on the scale of multiple eV [13]. Actinide L-edge spectroscopies can be very useful when configuration splittings are (rarely) observed in the final state [14], but are otherwise limited to measuring peak shifts and intensities that can be due to either delocalization or occupancy changes, potentially even due to non-f-orbitals [14–16]. The new, higher resolution variants of M-edge spectroscopies can also be successful probes of bonding [17–19], but are generally still reliant on edge shifts and fingerprinting techniques. In this article, we describe how a coupled use of $M_4$ and $M_5$ spectra collected in the high-energy-resolution fluorescence detection (HERFD) mode and properly normalized, can be used to separately determine the $5f_{5/2}$ and $5f_{7/2}$ unoccupied density of states (UDOS), providing a measure of the total 5f UDOS with higher resolution than previously possible.

Utilizing both the $M_4$ (3d$_{3/2}$) and $M_5$ (3d$_{5/2}$) edges, outlined below is a method of normalizing $M_4/M_5$ HERFD spectra that allows for the isolation of the $5f_{5/2}$ and $5f_{7/2}$ UDOS. This approach is based upon the strong electric dipole selection rules and cross section analysis that
drive the success of the Branching Ratio Analyses of X-ray Absorption Spectroscopy (XAS) [7,12,20–22]. An extensive analysis was performed, using the control samples of UF₄ (localized, two 5f electrons) and UCd₁₁ (localized, three 5f electrons) and comparing the measurements to the predictions of the Intermediate Coupling Model. [7,12] From the improved understanding garnered from the control experiment, and confirmed by comparison with the measurement of the UDOS provided by Bremsstrahlung Isochromat Spectroscopy [23–25], a form of high-energy Inverse Photoemission, the UDOS’s of U 5f⁵/₂ and U 5f⁷/₂ of UF₄ have been separately determined for the first time.

In this manuscript, the focus will be upon three 5f localized cases: UF₄, UCd₁₁, and UO₂. For now, delocalized systems such as U metal will not be addressed.

2. Experiment

The experiments were performed on Beamline 6-2a at the Stanford Synchrotron Radiation Lightsource, using a Si(111) monochromator and a high-resolution Johannson-type spectrometer [26] operating in the tender x-ray regime (1.5–4.5 keV). The total energy resolution of this HERFD experiment is 0.8 eV, sharpening the U M₄/M₅ spectroscopic features almost an order of magnitude when compared to conventional x-ray absorption spectroscopy (i.e., total fluorescence yield or transmission mode XAS). The samples used were the same as those used in earlier RXES and XAS studies. [22] Despite the conventional wisdom that tender x-ray experiments should in general have lessened surface sensitivity, more like hard x-rays than soft x-rays, the impact of surface oxidation for samples stored in air was immediately apparent, as also observed by Kvasninha et al. [19,27]. This sensitivity is due to the very intense x-ray absorption cross sections for U M-edges (for instance, the edge energy for U is 0.03 eV) and the propensity for uranium to react with oxygen. [28,29] However, by carefully measuring the U M₄₅ X-Ray Absorption Fine Structure (EXAFS) beyond the main (whiteline) absorption features, it was possible to monitor the oxidation levels. Ultimately, by employing freshly cleaved sample surfaces and keeping the samples isolated in an Ar atmosphere, this problem was eliminated in the present measurements. In fact, although similar, the EXAFS of the iso-electronic compounds, UF₄ and UO₂, are easily differentiated, consistent with earlier studies. [22] The efficacy and importance of the EXAFS will be discussed further below. The experimental data have been corrected for self-absorption effects, two examples of which are shown in Fig. 1 [30].

3. Results and discussion

To put the M₄ and M₅ spectra on the same energy and intensity scales, the procedure suggested by Rogalev was followed. [31,32] Here, the first step is to match the EXAFS across a wide energy regime, for each pair of spectra (M₄ and M₅) for a given sample. This normalization is shown for the UF₄ and UCd₁₁ spectra in the upper panels of Figs. 2. This process produces two white-line peaks that overlap and are separated by about 1 eV. The second step is to scale the M₄ and M₅ EXAFS regimes by their initial state densities: 2/3(M₄,3d₃/₂) to 1(M₅,3d₅/₂). An enlargement of the results of this procedure can be seen in Fig. 1.

To quantify the changes observed in Fig. 1 between UF₄ and UCd₁₁, peak fits were performed. (Lower panels, Fig. 2) Two asymmetric functions were used, each being a Gaussian with an exponential tail. Note that in Peak0, the tail extended to higher energy densities with the leading edge, and in Peak1, the tail pointed in the reverse direction captures the long tailing tail of the experimental spectrum. The results of the fit are shown in the lower panel of Fig. 2, including the experimental Peak Ratio, PR. (PR = Area(Peak0)/Area(Peak1))

Before going any further, it is necessary to discuss selection rules and cross sections. The strength of the selection rules has been demonstrated by the quantitative agreement in the Branching Ratio approach used in the conventional X-ray Absorption Spectroscopy (XAS) and Intermediate Coupling Model [7,12,20–22]. In the N₄,₅ conventional XAS, the lifetime broadening washes out any fine structure, leaving the cross section measurements as the only viable process [13]. However, within localized systems such as UF₄ and Pu, the jj-skewed Intermediate Coupling Model provides quantitative agreement with the experimental measurements. The jj-skewed Intermediate Coupling Model is based upon the selection rule that transitions between the 4d₃/₂ and 5f₇/₂ states are forbidden [33]. This selection rule is manifested in the M₄ notation in Fig. 1, which shows that the 3d₃/₂ electrons can only go into 5f₇/₂ unoccupied states. Thus, ignoring any quadrupole transitions that are much reduced in intensity, the M₄ HERFD experiment is probing directly the 5f₇/₂ Unoccupied Density of States or UDOS. For the M₅ case, it is slightly more complicated, but the process will be dominated by transitions from the 3d₅/₂ into the 5f₇/₂, since the relative cross section into an empty 5f manifold for a 3d₅/₂→5f₇/₂ transition is only 5% that of a 3d₅/₂→5f₇/₂ transition. With n = 2 and preferential filling of the 5f₇/₂ states, that ratio will drop to 3%. Thus, within a 3% error, it is possible to say that the M₅ experiment provides a measurement of only the 5f₇/₂ UDOS. (The small 5f₅/₂ contribution also helps explain why the M₅ is broader than the M₄.) In support of the contention that the M₄ intensity represents the 5f₅/₂ UDOS and the M₅ intensity represents the 5f₇/₂ UDOS, it is interesting to note the similarity of the spectra in Fig. 1 to the calculations of 5f₅/₂ UDOS and 5f₇/₂ UDOS of U by Kutepov [7] and the success of Kutepov’s calculations in recapitulating the essence of the UDOS measurements of U using Bremsstrahlung Isochromat Spectroscopy [7,23,34].

The dominant result shown in Fig. 1 is the large reduction in the main peak in the M₅ spectrum going from UF₄ to UCd₁₁. The first step to understanding this reduction is to consider the nominal spin-orbit split degeneracy, 6 for the 5f₅/₂ and 8 for the 5f₇/₂. In the case of n = 2, the 5f₅/₂ is 67% empty, while for n = 3, it is 50% empty, which is only a 25% reduction. The observed reduction is closer to 50%, and this could be explained if these nominally degenerated 6 states are further split into a series of doubly degenerate states. One possibility for this split transition could be the Crystal Field Splitting in UF₄ and UCd₁₁ [22,29,35,36]. The lower symmetry of these crystals would not support degeneracies above two-fold. A cartoon depicting this situation is shown in the inset of Fig. 2. It should be noted that the dominant effect in actinide 5f states is total angular momentum coupling in an Intermediate Coupling Model, which is skewed towards a jj-limit. (Among other things, the success of the Branching Ratio (BR) analysis of experimental results from localized systems such as UF₄ and Pu supports this contention [7,12,20–22]). Thus, a crystal field splitting of these states would result, in a first order perturbation, to split states but not mix states [22]. In this picture, the lowest doublet is filled for both UF₄ and UCd₁₁, allowing no intensity for the 3d₅/₂→5f₇/₂ transition. The second lowest doublet is either empty (UF₄, n = 2, N = 12) or ½ filled (UCd₁₁, n = 3, N = 11), where n + N = 14, with n = number of 5f electrons and N = number of 5f holes. The beauty of this picture is that the prior results for localized systems within the Intermediate Coupling Model can then be used to predict the expected Peak Ratios. [7] In such a model for n = 2: N₅/₂ = 6 - n₅/₂ = 6 - 1.96 = 4.04 and for n = 3, N₇/₂ = 6 - n₇/₂ = 6 - 2.79 = 3.21, using n₇/₂ + N₇/₂ = 6, with 5/2 designating the 5f₇/₂ manifold. The transition from n = 2 to n = 3 would then generate a change in the number of 5f/2 holes: ΔN₅/₂ = 4.04 - 3.21 = 0.83. It is reasonable to assume that for Peak0, ΔN₅/₂ = ½ of the initial number of holes in that level, 2(0.83) = 1.66. (Again, the n, n₅/₂, and n₇/₂ values are taken directly from the tables containing the Intermediate Model results in Ref. [7] and it is physically logical to assume that the filling process of going from n = 2 to n = 3 would change the number of holes in the states associated with Peak0 by a factor of 1/2.) Then, for n = 2, PR = 1.66/(4.04 - 1.66) = 0.70 and for n = 3, PR = 0.83/(4.04 - 1.66) = 0.35. These theoretical results agree nicely with the experimental results, as shown in the tabular insets in the lower panels of Fig. 2.
Above, it was briefly alluded that Bremsstrahlung Isochromat Spectroscopy, BIS, can provide a measure of the 5f UDOS, albeit with the loss of separate resolution of the 5/2 and 7/2 components and with poorer overall energy resolution [7,23–25,34]. BIS is the high energy variant of Inverse Photoelectron Spectroscopy. Just as X-ray Photoelectron Spectroscopy can provide a measure of the occupied density of states (ODOS), BIS can provide a measure of the UDOS. Next, a comparison will be made of a state-of-the-art BIS measurement with the HERFD results for UO₂ [24,25], as a final test of our model and contention that these HERFD measurements are an effective measure of the 5f UDOS.

For the sake of convenience and appearance, the EXAFS scaling between the M₄ and M₅ was set to 2/3 above, consistent with the initial state occupation ratios. However, a better quantitative scaling would be to use the ratio from the BR measurements. For UO₂, BR = 0.68 [14] and the M₄/M₅ EXAFS ratio would then be (1/BR) - 1 = 0.47, less than the value of 0.67 used earlier.

The result of such as scaling is shown in Fig. 3, along with the wide scan EXAFS matching for UO₂. As shown, there is a remarkable match between the M₄ + M₅ Sum and the BIS spectrum. At each change in slope in the BES spectrum, there is a corresponding change in slope of the M₄+M₅ spectrum, as denoted by the vertical orange lines. The HERFD sum is narrower, evidencing better energy resolution than the BIS, but exhibiting all the same fine structure. To test the effect of worsening the HERFD resolution, the HERFD data were convolved with a Gaussian function of 3 eV Full Width at Half Max. (The value of 3 eV was extracted from the 10%–90% width of the leading edge of the BIS spectrum and is roughly consistent with earlier resolution measurements of this BIS spectrometer [37]). The result is a loss of fine structure but an overall peak that matches the BIS spectrum closely. (Not shown.) Thus it is clear: the HERFD measurements provide a high resolution probe of the total 5f UDOS and a separation of the 5f⁵/₂ and 5f⁷/₂ UDOS of UO₂.

At this point, it is useful to put our results in context. Strictly speaking, HERFD, as being a cut of RIXS map, does not give a direct 1-to-1 measurement of the true unoccupied DOS. Rather, the full RIXS plane provides a detailed measure of the density of states convolved with the transition matrix elements via the Kramers-Heisenberg equation [38]. Making a cut through a RIXS spectrum using a constant emission energy, as is done to produce a HERFD spectrum, mimics
something that is linearly related to the UDOS for these samples, as we have demonstrated. However, for samples with a more complex electronic structure than the model compounds measured here (e.g. a mixed valence compound), it may be necessary to measure a full RIXS map. In any case, due to a combination of the choice of emission energy and self-absorption effects, there is a need to carefully determine the scattering geometry and thus use reasonably flat samples. Regarding the measurement of the DOS, there have been parallel discussions for XPS and BIS, over the decades. Strictly speaking, photoemission and inverse photoemission are measures of the joint density of states (initial and final) connected and moderated by electric dipole selection rules [39]. On that basis, one might argue that those factors in XPS and/or BIS cannot be deconvolved to directly provide the DOS. Nevertheless, there is an immense amount of data that supports the argument that, under many circumstances, XPS provides a very useful measure of the occupied density of states (ODOS) [40,41]. (The basis of this observation is probably a significant amount of angular and energy averaging, taking out directional effects and smoothing over cross-section variations.)

This capability is one of the reasons for the popularity of XPS as an analysis platform. More recent results for U metal, comparing the BIS of Baer and Lang with the calculations of Kutepov, demonstrate a similar success for BIS [7,23,34].

4. Conclusions and projections

We have shown that the HERFD/RIXS experiment performed at M4/ M5 edges is a powerful approach that is consistent with earlier traditional XAS BR investigations, the Intermediate Coupling Model and their underlying selection rules and provides an effective, high resolution measurement of the 5f_{5/2}, 5f_{7/2} and 5f total UDOS states in Uranium compounds. This approach can be applied broadly for Actinide elements to directly reveal their 5f-electrons properties.

While the nature of the additional splitting remains unknown at this point, one strong possibility is crystal field splitting. Conventional XAS Branching Ratio measurements have been shown to have negligible dependence upon crystal field splitting [22]. Nevertheless, the
improved resolution of the HERFD measurements has revealed the previously unavailable detail underlying the broadened spectra of conventional XAS. In a recently published article [42], the interplay of crystal-field splitting, spin-orbit splitting and total angular momentum coupling is addressed. Because the coulombic repulsion can cause energy differences between different total angular momentum states on the scale of 20 eV, it is conceivable that crystal-field splittings could be on the scale of 1–2 eV and still remain in the perturbative regime relative to the larger energy scale. The energy splittings that are observed here, in the $M_4$ and $M_5$ spectra, are on the scale of 1–2 eV. It is not the ratio of the crystal-field splitting to spin-orbit splitting that is the crucial parameter, but rather the ratio of crystal-field splitting to the energy differences between the total angular momentum states. The differences in energy between the total angular momentum states (20 eV) enforce the dominance of spin-orbit splittings, even though the spin-orbit splittings are on the order of 1–2 eV themselves. Finally, because the crystal-field splitting is still only perturbative relative to the energy differences of the total angular momentum states, cross-sectional measurements such as conventional XAS Branching Ratios will not be sensitive to crystal field splittings. That is because in First Order Perturbation Theory, states are split but not mixed, so the low resolution cross section measurements will sum the same, with or without the crystal-field splitting [42].

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